

Factoring Trinomials with a leading coefficient greater than 1.

Ex 1) $2x^2 + 7x - 15$ $GCF=1$

$$\begin{aligned} & \overbrace{2x^2 - 3x}^{-30} + \overbrace{10x - 15} \\ & x(2x - 3) + 5(2x - 3) \\ & (2x - 3)(x + 5) \end{aligned}$$

factors of -30	Sum of factors.
-2 x 15	-2 + 15 = 13
-3 x 10	-3 + 10 = 7 ✓

Ex 2) $6x^2 - 13x - 5$ $GCF=1$

$$\begin{aligned} & \overbrace{6x^2 + 2x}^{-30} - \overbrace{15x - 5} \\ & 2x(3x + 1) - 5(3x + 1) \\ & (3x + 1)(2x - 5) \end{aligned}$$

factors of -30	sum of factors.
-2 x 15	-2 + 15 = 13
2 x -15	2 + (-15) = -13 ✓

Ex 3) $6x^2 - 5x + 1$ $GCF=1$

$$\begin{aligned} & \overbrace{6x^2 - 2x}^{-3} - \overbrace{3x - 1} \\ & 2x(3x - 1) - 1(3x - 1) \\ & (2x - 1)(3x - 1) \end{aligned}$$

factors of 6	sum of factors
1 x 6	1 + 6 = 7
2 x 3	2 + 3 = 5
-2 x -3	-2 + (-3) = -5 ✓

Ex 4) $4x^2 + 4x + 1$ $GCF=1$

$$\begin{aligned} & \overbrace{4x^2 + 2x}^4 + \overbrace{2x + 1} \\ & 2x(2x + 1) + 1(2x + 1) \\ & (2x + 1)(2x + 1) \text{ Perfect Square Trinomial} \\ & (2x + 1)^2 \end{aligned}$$

factors of 4	Sum of factors
2 x 2	2 + 2 = 4

Ex 5) $18x^2 - 12x + 4$ GCF = 2

$2(9x^2 - 6x + 2)$

Doesn't factor.

factors of 18	sum of factors.
3x6	3+6 = 9
-3x-6	-3+(-6) = -9
1x18	1+18 = 19
-1x-18	-1+(-18) = -19
2x9	2+9 = 11
-2x-9	-2+(-9) = -11

Ex 6) $2(x+4)^2 - 11(x+4) + 15$ Let $b = x+4$

$2b^2 - 11b + 15$ GCF = 1

$2b^2 - 6b - 5b + 15$
 $2b(b-3) - 5(b-3)$
 $(b-3)(2b-5)$

factors of 30	sum of factors -11
2x15	
-2x-15	
3x10	
-3x-10	
1x30	
-6x5	-6+(-5) = -11

Ex 7) $(x^2 - 6)^2 + 7(x^2 - 6) - 30$ $b = x^2 - 6$

$b^2 + 7b - 30$

$b^2 + 10b - 3b - 30$
 $b(b+10) - 3(b+10)$

$(b+10)(b-3)$

Substitute $b = x^2 - 6$

$(x^2 - 6 + 10)(x^2 - 6 - 3)$

$(x^2 + 4)(x^2 - 9) \rightarrow$ Can this factor further?

$(x^2 + 4)(x + 3)(x - 3)$

factors of -30	sum of factors
-10x3	-10+3 = -7
10x-3	10+(-3) = 7 ✓

Pg. 258 #6

Assignment

a) $x^2 - 2x - 3$

g) $2x^2 - 72$

h) $\frac{1}{4}x^2 - \frac{1}{49}y^2$

b) $3x^2 + 5x - 2$

i) $0.81x^2 - 0.25$

c) $x^2 + 5x + 4$

j) $4(x+3)^2 + 8(x+3) - 5$

d) $2x^2 + 7x - 15$

k) $9(x-1)^2 - 100(x+1)^2$

e) $6x^2 + x - 2$

l) $(2x-1)^2 + 16(2x-1) + 63$

f) $5x^2 + 5x - 60$

